

Introduction to Functions

**What is a function?**  
It is a rule that will give **one and only one possible answer (y)** for any x value that is input into the rule.

**Function Notation:**  
Instead of y we use  $f(x)$  or  $g(x)$  or  $h(x)$  etc  
This is pronounce  $f$  of  $x$  or  $g$  of  $x$  or  $h$  of  $x$ ....

Let's look at an example of a linear function: a rule that will make a straight line

$f(x) = 2x + 8$  this could also be written  $y = 2x + 8$

Function notation allows us to ask a question using as few words as possible

*Example:  $f(3)=?$*   
(The question is asking us to plug 3 in for x and then solve for y... )

$$\begin{aligned} f(x) &= 2x + 8 & y = ax + b \\ f(3) &= 2(3) + 8 & f(x) = ax + b \\ &= 6 + 8 \\ &= 14 \end{aligned}$$

$$\begin{aligned} f(5) &= 18 & 2(5) + 8 \\ f(10) &= 28 & 2(10) + 8 \\ f(0) &= 8 & 2(0) + 8 \\ f(-2) &= -4 & 2(-2) + 8 \end{aligned}$$

Dec 7-7:21 PM

Think of the rule as a program: x is the input and y is the output

Example 2:  $g(x) = -3x + 10$

	Input x	Rule $g(x) = -3x+10$	Output y
$g(3)$	3	$-3(3)+10$	1
$g(2)$	2	$-3(2)+10$	4
$g(1)$	1	$-3(1)+10$	7
$g(0)$	0	$-3(0)+10$	10
$g(-1)$	-1	$-3(-1)+10$	13
$g(-2)$	-2	$-3(-2)+10$	16
$g(-3)$	-3	$-3(-3)+10$	19
$g(-11)$	-11	$-3(-11)+10$	43

} 3  
} 3  
} 3  
} 3

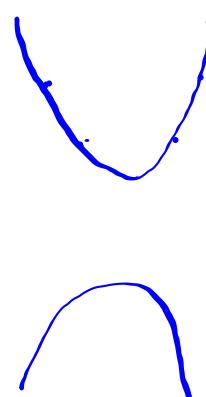
Dec 7-7:22 PM

Example 3

$$h(x) = 4x^2$$

Quadratic

	Input x	Rule $h(x) = 4x^2$	Output y
$h(3)$	3	$4(3)^2$	36
$h(2)$	2	$4(2)^2$	16
$h(1)$	1	$4(1)^2$	4
$h(0)$	0	$4(0)^2$	0
$h(-1)$	-1	$4(-1)^2$	4
$h(-2)$	-2	$4(-2)^2$	16
$h(-3)$	-3	$4(-3)^2$	36



Dec 7-7:24 PM

When we create a table for the function we can use the x (input) and y (output) together as pairs and use them to graph the function.

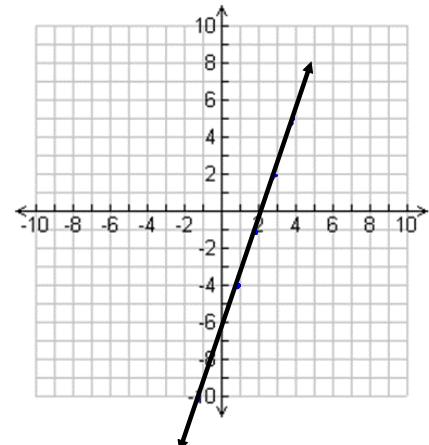
Create a table for the given rules. Choose values for x, input the value into the rule to determine the y.

Plot the pairs of coordinates and draw a line to represent the function.

Dec 7-7:24 PM

1)  $f(x) = 3x - 7$

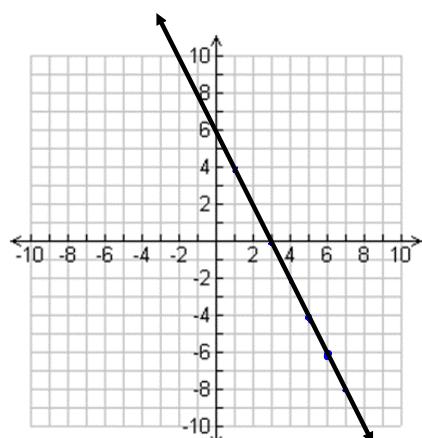
Input x	Rule $3x - 7$	Output y
$f(-2)$	$3(-2) - 7$	-13
$f(3)$	$3(3) - 7$	2
$f(2)$	$3(2) - 7$	-1
$f(1)$	$3(1) - 7$	-4
$f(-1)$	$3(-1) - 7$	-10
$f(4)$	$3(4) - 7$	5



Dec 7-7:26 PM

2)  $g(x) = -2x + 6$

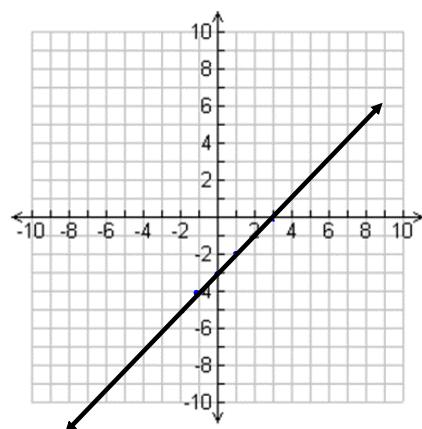
Input x	Rule	Output y
$g(3)$	$-2(3) + 6$	0
$g(1)$	$-2(1) + 6$	4
$g(7)$	$-2(7) + 6$	-8
$g(4)$	$-2(4) + 6$	-2
$g(6)$	$-2(6) + 6$	-6
$g(5)$	$-2(5) + 6$	-4



Dec 7-7:27 PM

3)  $f(x) = x - 3$

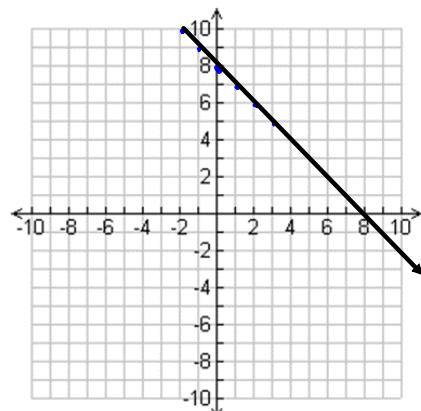
Input x	Rule	Output y
$f(3)$	$(3) - 3$	0
$f(2)$	$(2) - 3$	-1
$f(1)$	$(1) - 3$	-2
$f(0)$	$(0) - 3$	-3
$f(-1)$	$(-1) - 3$	-4
$f(-2)$	$(-2) - 3$	-5



Dec 7-7:27 PM

4)  $g(x) = -x + 8 \quad = \quad -1x + 8$

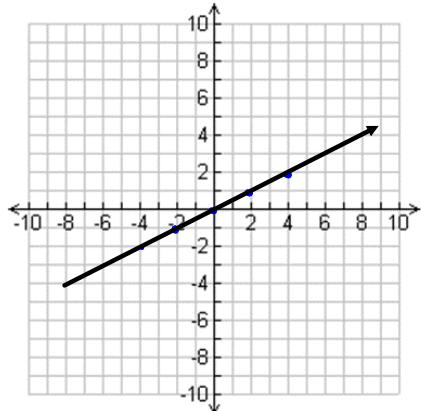
Input x	Rule	Output y
$g(-2)$	$-(-2) + 8$	10
$g(-1)$	$-( -1 ) + 8$	9
$g(0)$	$-( 0 ) + 8$	8
$g(1)$	$-( 1 ) + 8$	7
$g(2)$	$-( 2 ) + 8$	6
$g(3)$	$-( 3 ) + 8$	5



Dec 7-7:28 PM

5)  $f(x) = 0.5x$   $\leftarrow \frac{1}{2}x$  Multiples

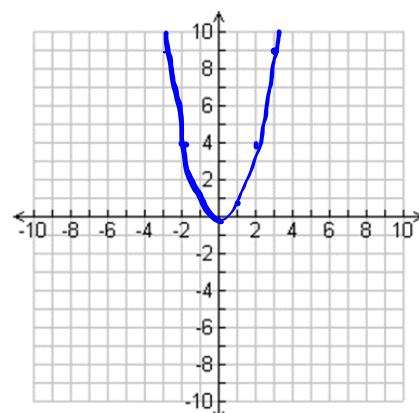
Input x	Rule	Output y
$f(-4)$	$0.5(-4)$	-2
$f(-2)$	$0.5(-2)$	-1
$f(0)$	$0.5(0)$	0
$f(2)$	$0.5(2)$	1
$f(4)$	$0.5(4)$	2



Dec 7-7:28 PM

6)  $h(x) = (x^2)$

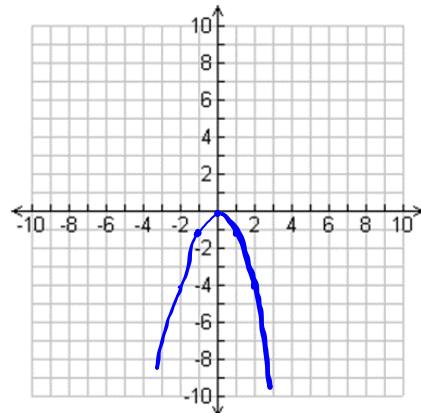
Input x	Rule	Output y
-3	$(-3)^2$	9
-2	$(-2)^2$	4
-1	$(-1)^2$	1
0	$0^2$	0
1	$(1)^2$	1
2	$(2)^2$	4
3	$(3)^2$	9



Dec 7-7:29 PM

7)  $g(x) = -(x^2)$   $\therefore -1(x^2)$

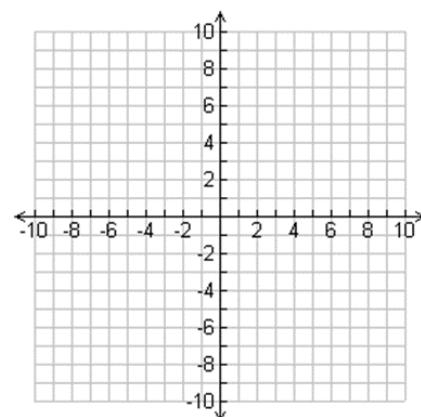
Input x	Rule	Output y
-2	$-( -2 )^2$	-4
-1	$-( -1 )^2$	-1
0	$-( 0 )^2$	0
1	$-( 1 )^2$	-1
2	$-( 2 )^2$	-4



Dec 7-7:29 PM

8)  $h(x) = 0.5(x^2)$

Input x	Rule	Output y
-4		
-2		
-1		
0		
1		
2		
-4		



Dec 7-7:29 PM

Homework

Textbook #2

P30 #1

P31 #5

Dec 9-5:24 PM