

Geometry Review

Types of triangles:

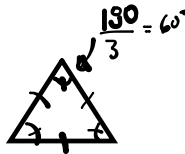
Isosceles



Characteristics:

2 congruent
- sides
- angles

Equilateral



3 congruent
- sides
- angles

Scalene



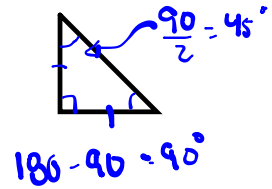
3 diff
- sides
- angles

Right



1 angle = 90°

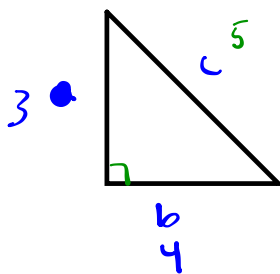
$a^2 + b^2 = c^2$
hypotenuse



The sum of angles in any triangle is = 180°

Pythagoras Theorem

Find hypotenuse:



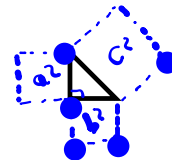
$$a^2 + b^2 = c^2$$

$$3^2 + 4^2 = c^2$$

$$9 + 16 = c^2$$

$$\sqrt{25} = \sqrt{c^2}$$

$$5 = c$$



3, 4, 5

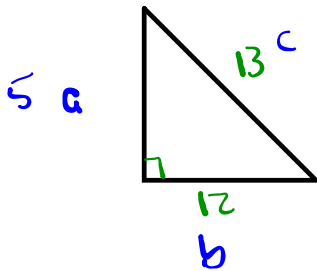
6, 8, 10

9, 12, 15

30, 40, 50

Pythagoras Theorem (cont'd)

Find missing leg:



$$a^2 + b^2 = c^2$$

$$c^2 - a^2 = b^2$$

$$c^2 - b^2 = a^2$$

$$13^2 - 12^2 = a^2$$

$$169 - 144 = a^2$$

$$\sqrt{25} = \sqrt{a^2}$$

$$5 = a$$

$$n = \# \text{ sides}$$

$$(n-2) \times 180$$

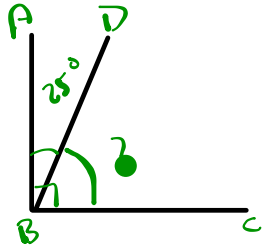
Quadrilaterals

$$\sum \text{ angles} = 360^\circ$$

Type	Properties
<p>Parallelogram</p>	<ul style="list-style-type: none"> • Opposite sides are equal and parallel • Opposite angles are equal
<p>Rectangle</p>	<ul style="list-style-type: none"> • Opposite sides are equal and parallel • All angles are right angles (90°)
<p>Square</p>	<ul style="list-style-type: none"> • Opposite sides are parallel • All sides are equal • All angles are right angles (90°)
<p>Rhombus</p>	<ul style="list-style-type: none"> • Opposite sides are parallel • All sides are equal • Opposite angles are equal • Diagonals bisect each other at right angles (90°) - perpendicular
<p>Trapezoid</p>	<ul style="list-style-type: none"> • One pair of opposite sides is parallel
<p>Kite</p>	<ul style="list-style-type: none"> • Two pairs of adjacent sides are equal • One pair of opposite sides are equal • One diagonal bisects the other • Diagonals intersect at right angle (90°)

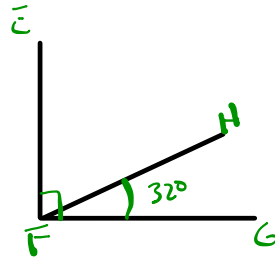
Angles

Complementary angles: $\text{Angles} = 90^\circ$



$$\angle DBC = 90^\circ - 25^\circ = 65^\circ$$

Comp. Angles



$$\angle HFG = 32^\circ$$

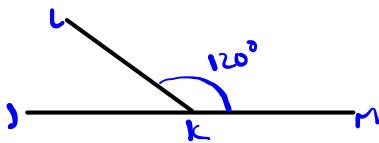
What is $\angle EFH$?

$$90^\circ - 32^\circ = 58^\circ$$

$$\angle EFH = 58^\circ - \text{Comp. Angles}$$

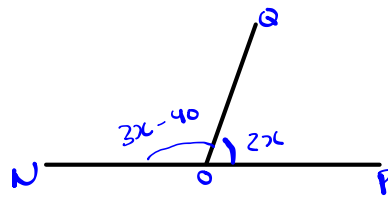
Angles

Supplementary angles: $\text{Angles} = 180^\circ$ (Straight line) $\angle = \text{angle}$



$$\angle JKL ? \quad 180^\circ - 120^\circ = 60^\circ$$

$$\angle JKL = 60^\circ - \text{Sup Angles}$$



$$\angle NOQ = 3x - 40$$

$$3x - 40 + 2x = 180 \quad - \text{Sup Ang}$$

$$5x - 40 = 180 + 40$$

$$5x = 220$$

$$\frac{5x}{5} = \frac{220}{5}$$

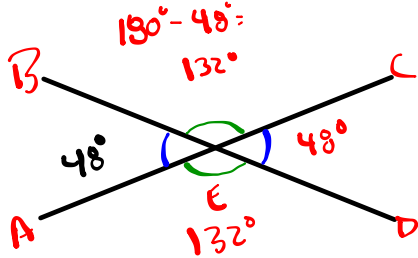
$$x = 44$$

$$\angle NOQ = 3(44) - 40 = 92^\circ$$

$$\angle QOP = 2(44) = 88^\circ$$

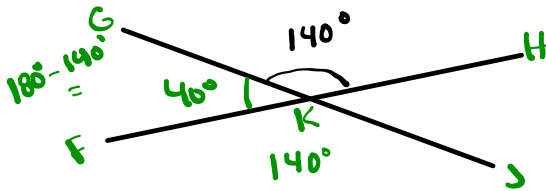
Angles L

Vertically Opposite angles (VOA):



$\angle CED = 48^\circ$
 $\angle BEC = 132^\circ$
 $\angle AED = 132^\circ$

VOA
 Supp. Angles
 VOA



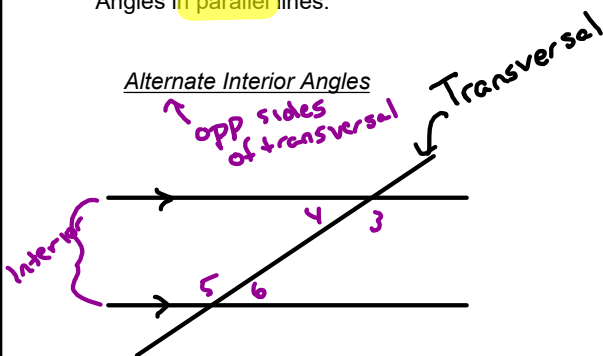
$\angle FKJ = 140^\circ$
 $\angle FKG = 40^\circ$
 $\angle HKJ = 40^\circ$

VOA
 Supp. Angles
 VOA

Angles

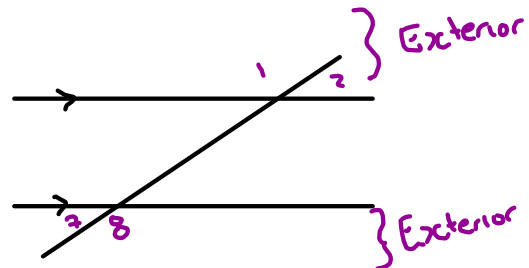
Angles in parallel lines:

Alternate Interior Angles



$\angle 4 = \angle 6$
 $\angle 3 = \angle 5$

Alternate Exterior Angles



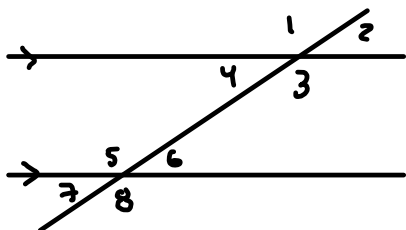
$\angle 1 = \angle 8$
 $\angle 2 = \angle 7$

Ex: $\angle 5 = 133^\circ = \angle 3$ - Alt Int. Ang.
 $\angle 4 = 180^\circ - 133^\circ = 47^\circ$ - Supp. Ang.
 $\angle 6 = 47^\circ$ - Alt Int. Ang.

Angles

Angles in parallel lines:

Corresponding Angles



- Same side of transversal
- 1 interior + 1 exterior angles

$$\angle 1 = \angle 5$$

$$\angle 4 = \angle 7$$

$$\angle 2 = \angle 6$$

$$\angle 3 = \angle 8$$