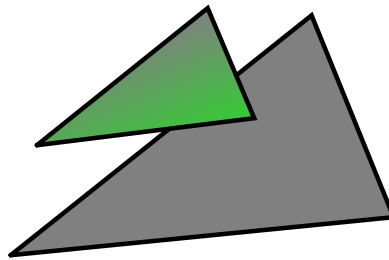
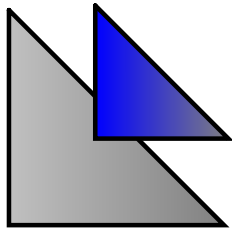
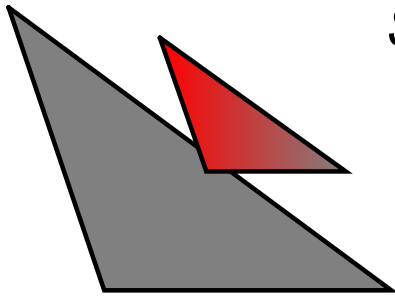


Triangle Geometry

Similar Triangles



Mar 23-10:15 AM

similarity has a lot to do
with
proportionality

the mathematical understanding of
SIMILAR is different than our
"normal" understanding of the word

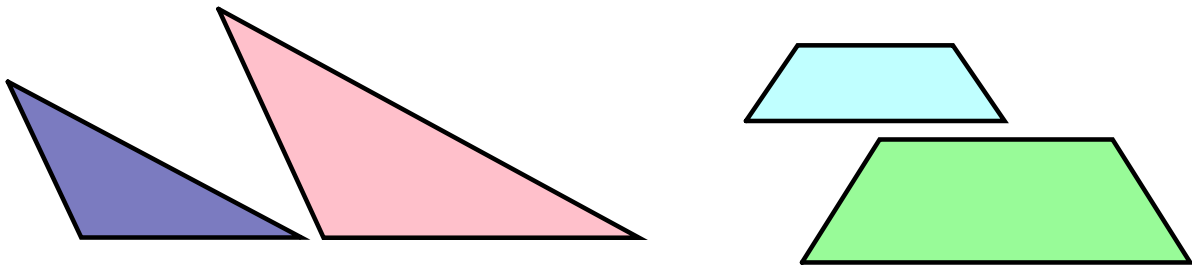
Mar 23-12:28 PM

Two figures are considered **SIMILAR** if:

....they have the same **shape**

....the corresponding **angles** are **congruent**

....the corresponding **sides** are **proportional**

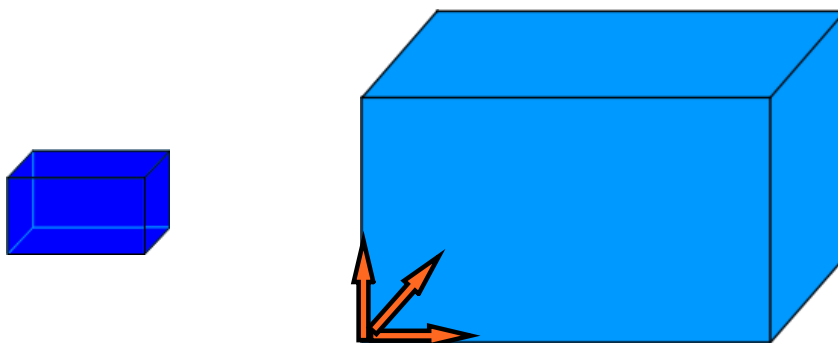


All three of the above conditions must be met

Mar 23-10:16 AM

When things grow **proportionally**, we say that they grow in all dimensions by the **same factor**


if something gets **three** times as wide, it will also get three times as tall and three times as deep



Mar 23-12:20 PM

If two parallelograms are proportional, then the corresponding sides are larger (or smaller) by the same **factor**.

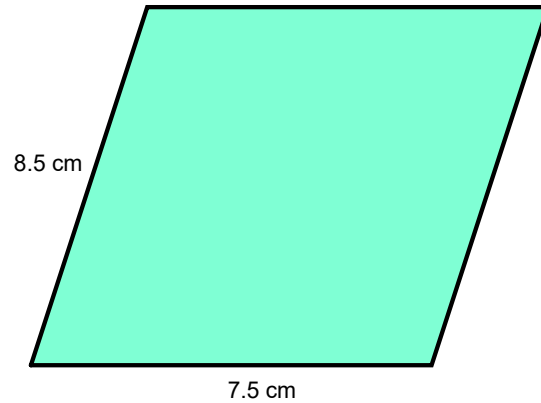
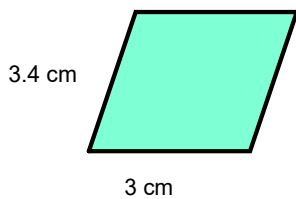
scale factor = $\frac{5}{2}$



$$\frac{3.4}{8.5} = \frac{3}{7.5} = \frac{2}{5}$$

scale factor = $\frac{2}{5}$





these are proportional

increasing the size, then $k > 1$ decreasing the size, then $k < 1$

Mar 23-12:28 PM

A **proportion** is made of two equal ratios (fractions)

$$\frac{1}{2} = \frac{2}{4}$$

from the previous page: $\frac{3.4}{8.5} = \frac{3}{7.5} =$

$\frac{\text{the measure of a side from "the first" figure}}{\text{the measure of its corresponding side in the second figure}}$
--

Mar 23-10:19 AM

$$\frac{a}{b} = \frac{c}{d}$$

a proportion

after we cross multiply,
these will be equal

$$ad = bc$$

ex

$$\frac{3.4}{8.5} = \frac{3}{7.5}$$

$$3.4(7.5) \stackrel{?}{=} 8.5(3)$$

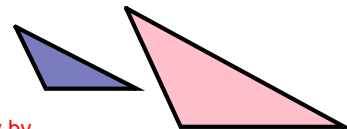
$$25.5 = 25.5$$

Mar 23-10:24 AM

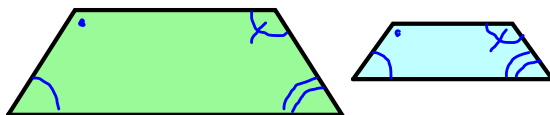
Two figures are considered **SIMILAR** if

....they have the same **shape**

this you can verify by
looking...is it a triangle,
trapezoid, square etc...

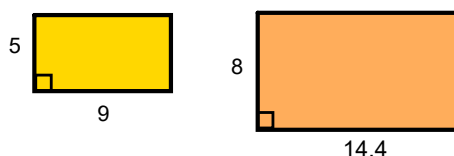


....the corresponding angles are **congruent**



this you can verify
mathematically ...the
measures are either
given or can be
calculated or deduced

....the corresponding sides are **proportional**



this you can verify
mathematically ...set up a
proportion

Mar 23-10:16 AM

Remember!

Once a **triangle** has been proven to be similar to another triangle, then you know two things:

- corresponding angles are **congruent**
- corresponding sides are **proportional**

Mar 23-6:28 PM

Like proving
congruence...we also
have **minimum
conditions** to *prove*
SIMILARITY

Mar 23-10:50 AM

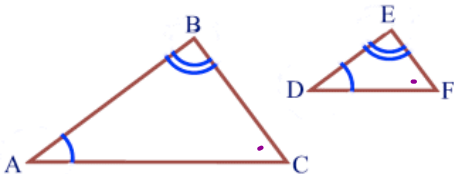
3 ways to prove that triangles are similar: ~

- 1. AA -- angle-angle
- 2. SSS_{prop} -- side-side-side (prop)
- 3. SAS_{prop} -- side-angle-side (prop)

Mar 23-12:52 PM

1. Proving triangles are similar by AA

Angle-Angle



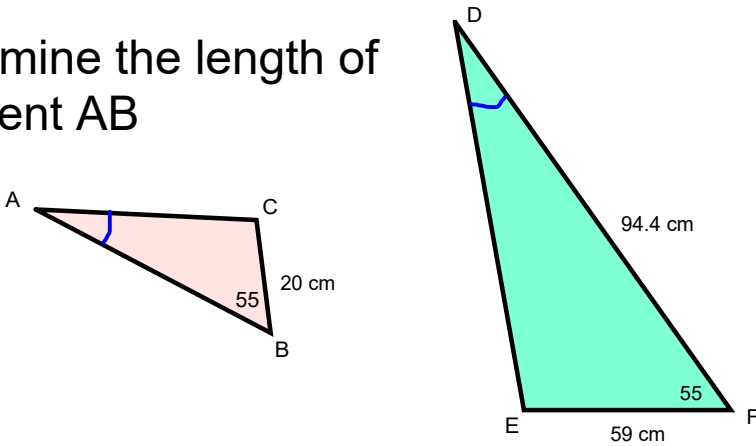
	statement	Justification
1		
2		
3		



Mar 23-12:45 PM

Example of a question:

Determine the length of segment AB



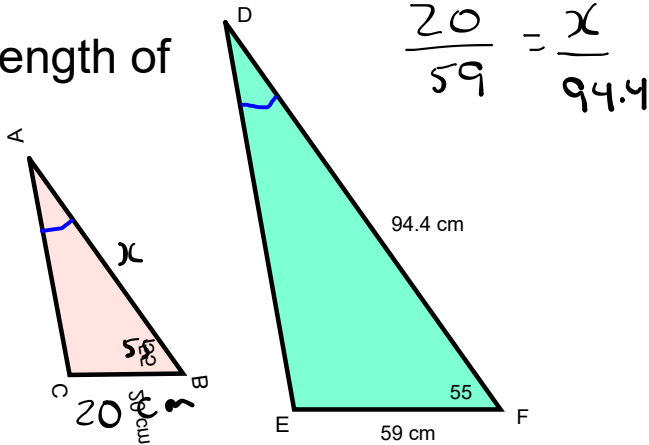
Step 1: Redraw the triangles so that both have the same orientation

Mar 23-12:50 PM

Example of a question:

Determine the length of segment AB

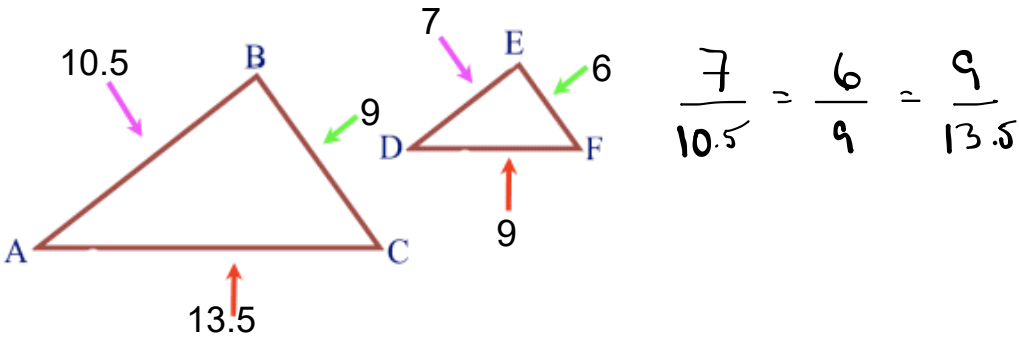
$$\frac{\overline{CB}}{\overline{EF}} = \frac{\overline{AB}}{\overline{DF}}$$



	statement	justification
A	1 $\angle BAC \cong \angle EDF$	Given
A	2 $\angle ABC \cong \angle EFD$	Given
	3 $\triangle ABC \sim \triangle DEF$	AA
	4 $\overline{AB} = 32\text{ cm}$	$\frac{20}{59} = \frac{x}{94.4}$ Corres. sides in similar \triangle are prop

Mar 23-12:50 PM

2. Proving triangles are similar by **SSSprop**
side-side-side (prop)



	Statement	Justification

Mar 23-12:50 PM

Example of a question: Prove that

Diagram showing two triangles, ABC and DEF, with side lengths. Triangle ABC has sides AB=96, BC=145.6, and AC=174.4. Triangle DEF has sides DE=60, EF=91, and DF=109. A right angle is marked at vertex B in triangle ABC and at vertex D in triangle DEF.

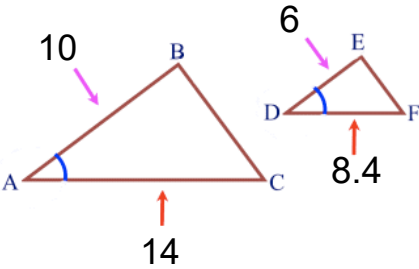
Handwritten notes:

$$a^2 + b^2 = c^2$$
$$96^2 + 60^2 = 174.4^2$$

	statement	justification
1	$\frac{ED}{AB} = \frac{DF}{AC}$	$\frac{60}{96} = \frac{91}{174.4}$ Corr sides
2	$\frac{EF}{BC} = \frac{DE}{AB}$	$\frac{60}{109} = \frac{91}{174.4}$ Corr sides
3	$\frac{DF}{BC} = \frac{EF}{AC}$	$\frac{91}{145.6} = \frac{109}{174.4}$ Corr sides
4	$\triangle ABC \sim \triangle DEF$	SSS prop
5	$\angle C \cong \angle F$	Corr angles in similar triangles

Mar 23-12:51 PM

3. Proving triangles are similar by **SASprop**
side-angle-side (prop)

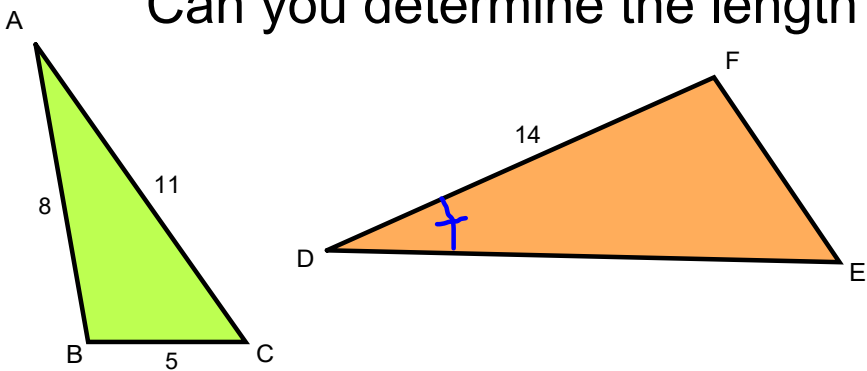


	statement	justification

Mar 23-12:51 PM

Example of a question:

Can you determine the length of \overline{EF} ?

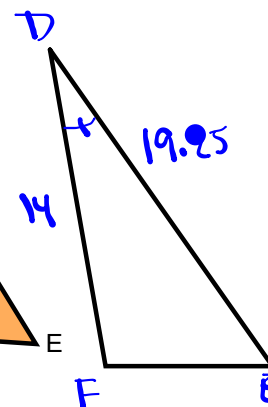
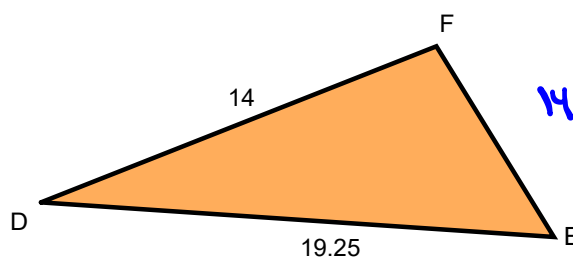
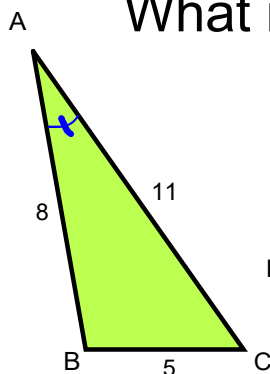


	statement	justification

Mar 23-12:54 PM

Example of a question:

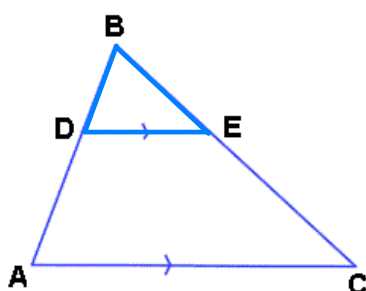
What is the length of \overline{EF} ?



	statement	justification
1	$\frac{AB}{DF} = \frac{AC}{DE}$	$\frac{8}{14} = \frac{11}{19.25}$

Mar 23-12:54 PM

Dealing with OVERLAPPING TRIANGLES



Many problems involving similar triangles have one triangle **ON TOP OF** (overlapping) another triangle.

Here we have $\triangle BDE$ and $\triangle BAC$

In this case line segments DE and AC are shown to be parallel--note the arrows on the line segments.

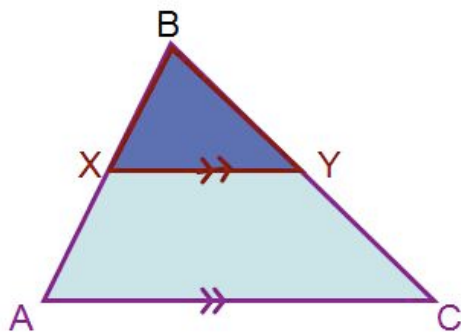
so,
we know that $\angle BDE$ is congruent to $\angle DAC$ (by corresponding angles).

$\angle B$ is shared by both triangles

so the two triangles are similar by AA

Mar 23-12:54 PM

Parallel Line to a Triangle's Side: Any line parallel to a triangle's side determines two similar triangles.



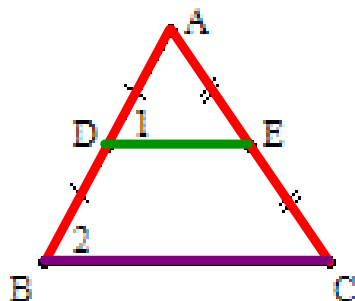
$$\triangle BXY \sim \triangle BAC$$

angles are congruent
sides are proportional

Corollary: Any two similar triangles determine parallel lines.

Mar 22-4:16 PM

Segment Joining the Midpoints of Two Sides in a Triangle: Any **segment** joining the midpoints of **two sides** in a triangle is parallel to the **third side** and is half the measure of this third side.



In triangle ABC

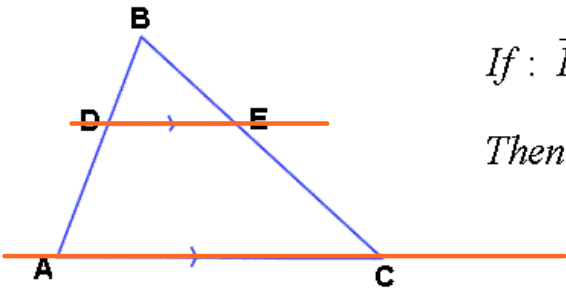
If: $AD = DB, AE = EC$

Then: $DE \parallel BC$

$$\overline{DE} = \frac{1}{2} \overline{BC}$$

Mar 23-2:01 PM

Thales' Theorem: Two intersecting transversal lines intersected by parallel lines are separated into corresponding segments of proportional length.

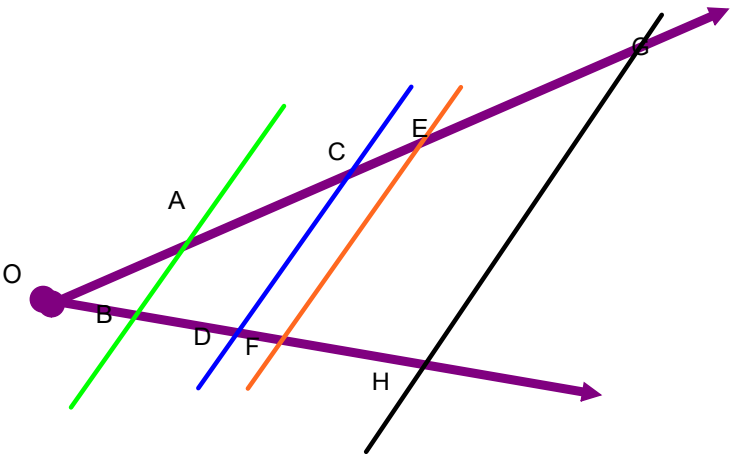


If : $\overline{DE} \parallel \overline{AC}$
Then : $\frac{BD}{DA} = \frac{BE}{EC}$

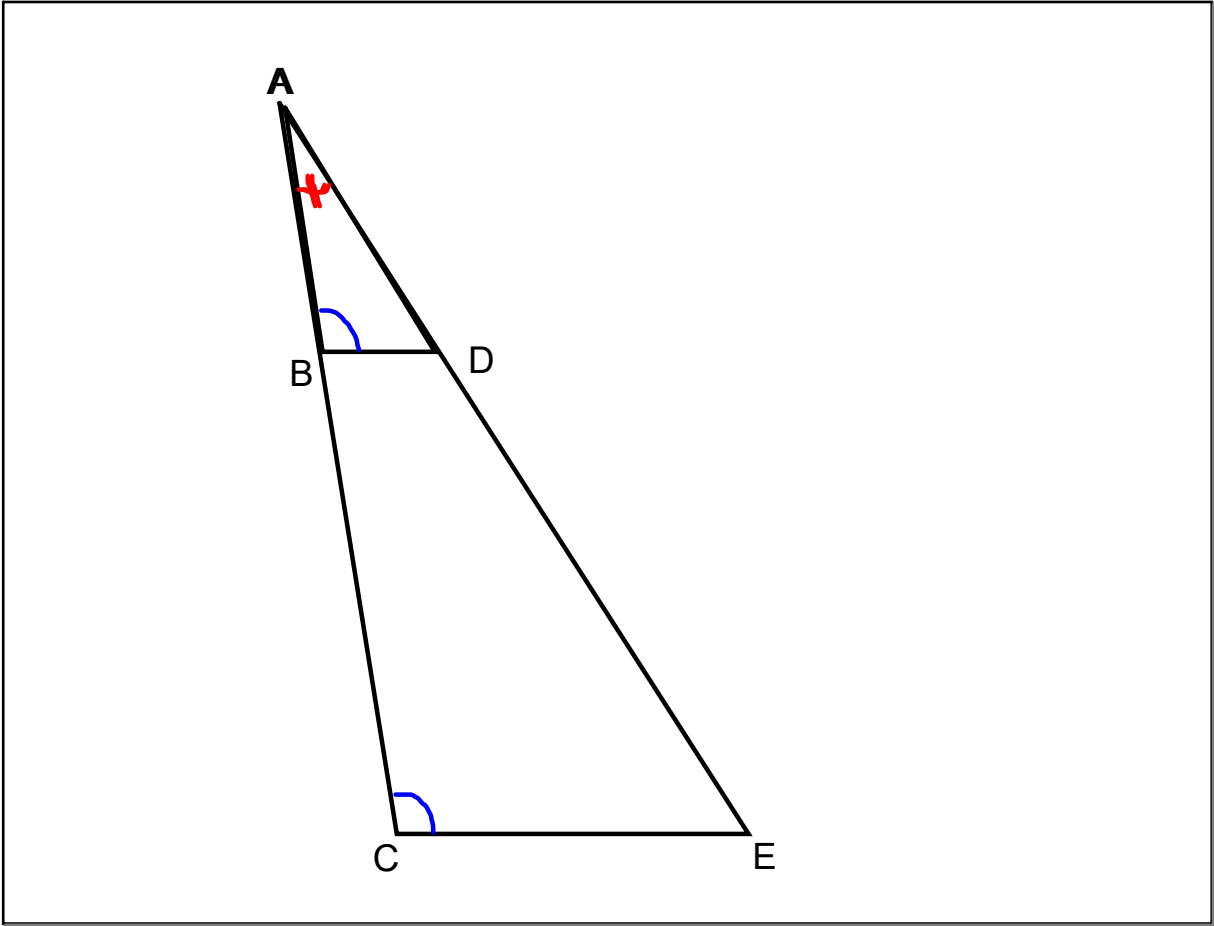
Mar 23-2:01 PM

Does not have to be a triangle

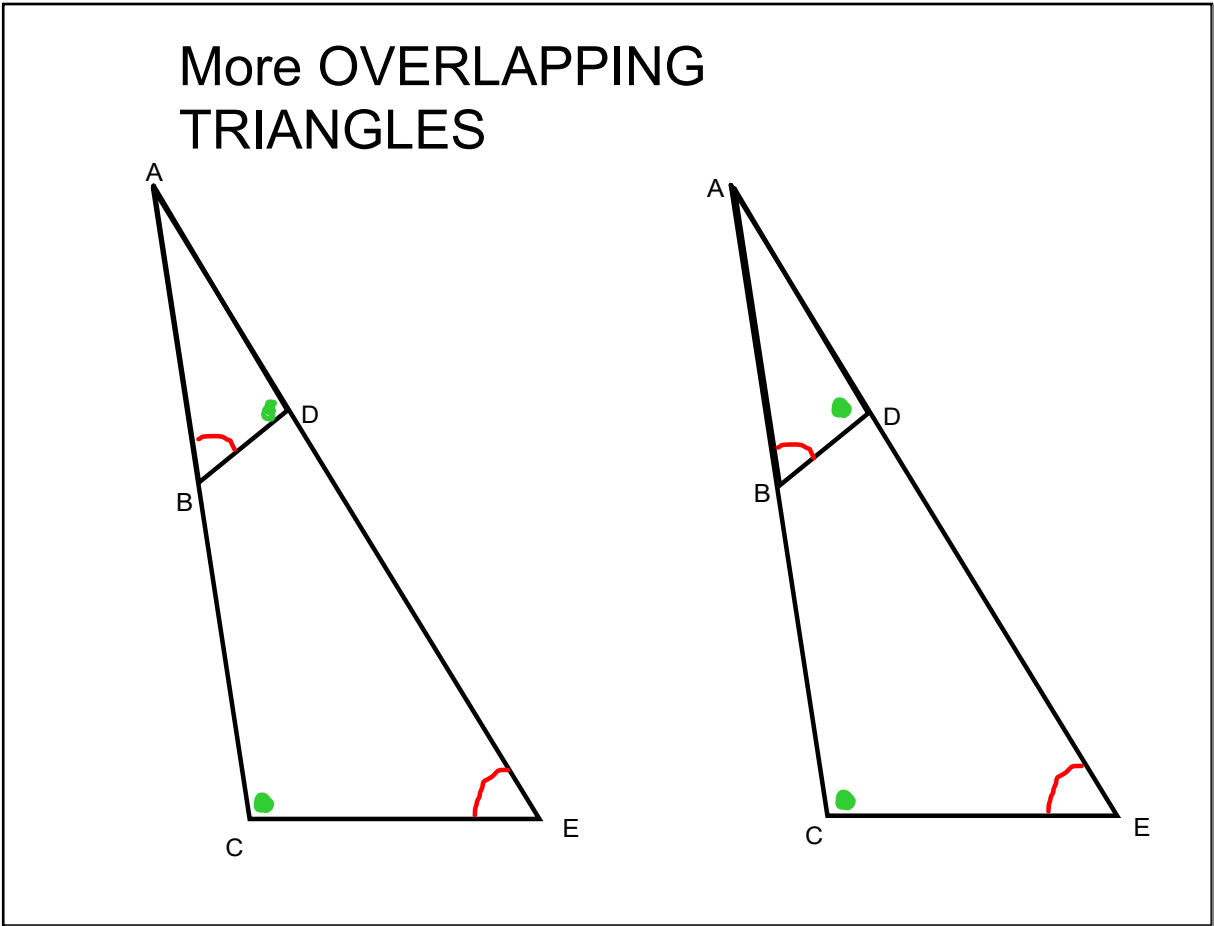
Lines AB CD EF GH



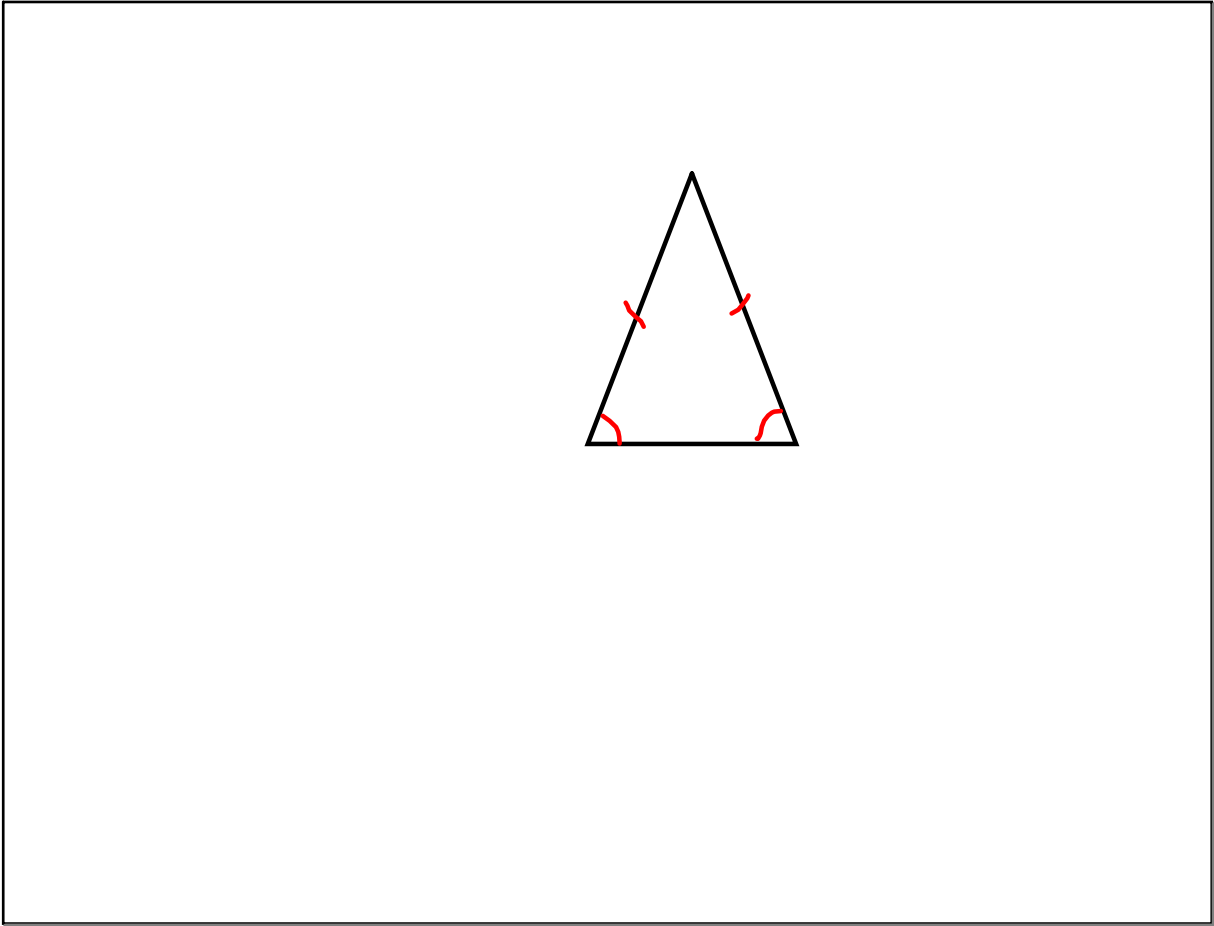
Mar 23-2:04 PM



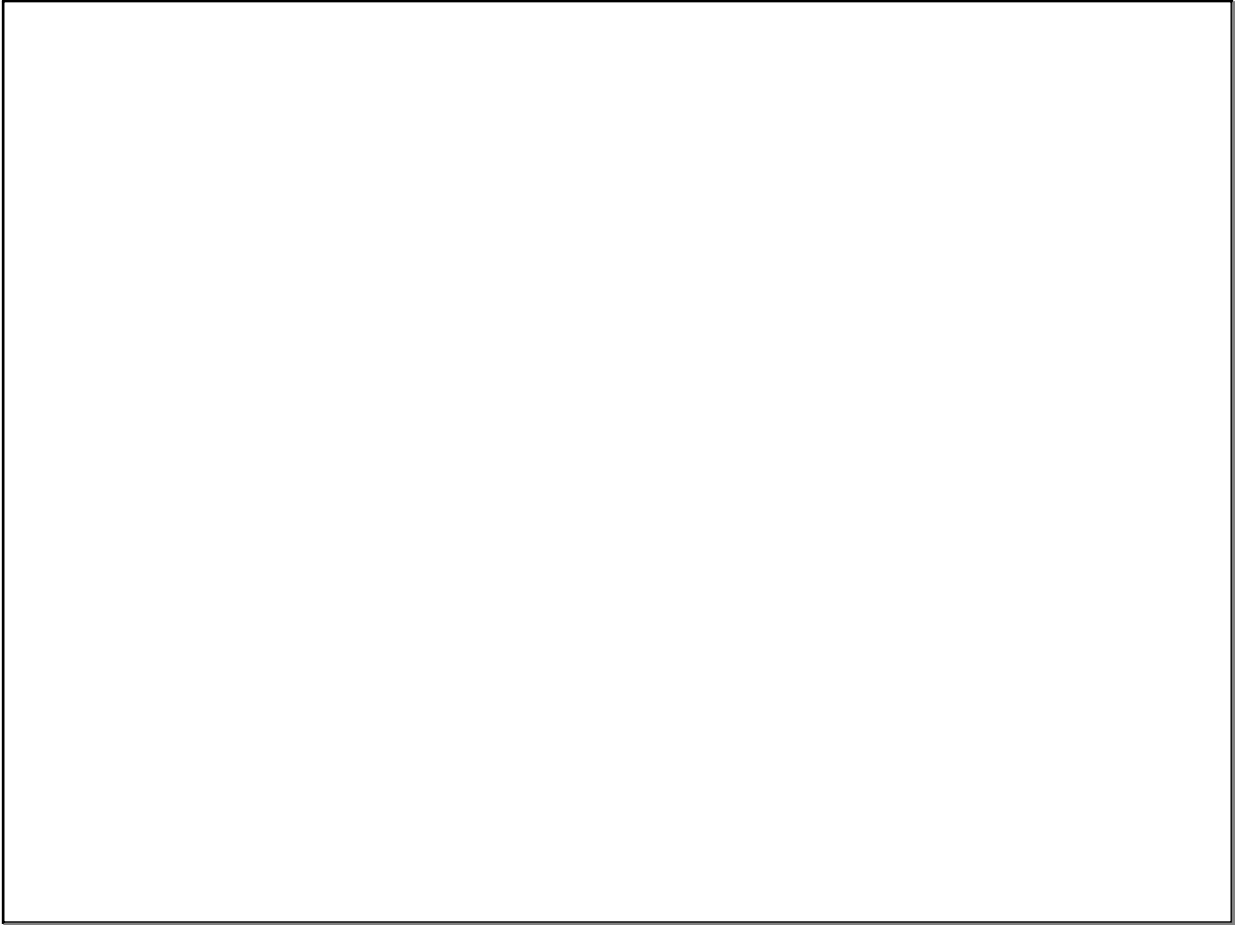
Mar 23-1:52 PM



Mar 23-1:56 PM



Mar 22-4:17 PM



Mar 23-2:02 PM